

නව නිර්දේශය/புதிய பாடத்திட்டம்/New Syllabus

ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව
 திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம்
 Department of Examinations, Sri Lanka
 இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம்
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අධ්‍යයන පොදු සහතික පත්‍ර (උසස් පෙළ) විභාගය, 2020
 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020
 General Certificate of Education (Adv. Level) Examination, 2020

සංයුක්ත ගණිතය I
 இணைந்த கணிதம் I
 Combined Mathematics I

10 E I

පැය තුනයි
 மூன்று மணித்தியாலம்
 Three hours

අමතර කියවීමේ කාලය - මිනිත්තු 10 යි
 மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள்
 Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

Index Number

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- * This question paper consists of two parts;
Part A (Questions 1 - 10) and **Part B** (Questions 11 - 17).
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 Answer **all** questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.
- * **Part B:**
 Answer **five** questions only. Write your answers on the sheets provided.
- * At the end of the time allotted, tie the answer scripts of the two parts together so that **Part A** is on top of **Part B** and hand them over to the supervisor.
- * You are permitted to remove **only Part B** of the question paper from the Examination Hall.

For Examiners' Use only

(10) Combined Mathematics I		
Part	Question No.	Marks
A	1	
	2	
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B	11	
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Total

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In Words	

Code Numbers

Marking Examiner	
Checked by:	1
	2
Supervised by:	

Part A

1. Using the Principle of Mathematical Induction, prove that $\sum_{r=1}^n (4r+1) = n(2n+3)$ for all $n \in \mathbb{Z}^+$.

[illegible]

- 2. Sketch the graphs of $y=3|x-1|$ and $y=|x|+3$ in the same diagram.**

Hence or otherwise, find all real values of x satisfying the inequality $3|2x-1| > 2|x|+3$.

[illegible]

3. Sketch, in the same Argand diagram, the loci of the points that represent the complex numbers z satisfying

(i) $\text{Arg}(z + 1 - 3i) = -\frac{\pi}{4}$ and

(ii) $|z - 2| = \sqrt{2}$.

Hence, write down the complex numbers represented by the points of intersection of these loci.

[illegible]

4. Let $n \in \mathbb{Z}^+$. Write down the binomial expansion of $(1+x)^n$ in ascending powers of x . Show that if the coefficients of two consecutive terms of the above expansion are equal, then n is odd.

[illegible]

[illegible]

- [illegible]

- Find the y -intercept of the normal line drawn to the above ellipse at the point $\left(\frac{5}{2}, \frac{3\sqrt{3}}{2}\right)$ on it.

This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- It is given that the perpendicular distance from the point $B \equiv (2, 3)$ to the line l is $\frac{1}{\sqrt{5}}$ units. Find the values of m .

[illegible]

- Hence**, show that the x -coordinates of the points of contact of the tangents drawn to S from A satisfies the equation $5x^2 + 8x + 2 = 0$.

[illegible]

- Using the identity $\cos^2 \theta + \sin^2 \theta = 1$, show that $\sec^2 \theta = 1 + \tan^2 \theta$.

Hence, show that $\cos \theta = \frac{24}{25}$.

This image shows a full page of white paper with horizontal dotted lines, typical of primary school handwriting practice paper. The lines are evenly spaced and run across the entire width of the page. There are no margins, text, or other markings present.

13.(a) Let $A = \begin{pmatrix} a+1 & 0 \\ 1 & 1 \\ 0 & 1 \end{pmatrix}$, $B = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ a & 2 \end{pmatrix}$ and $C = \begin{pmatrix} a & 1 \\ a & 2 \end{pmatrix}$, where $a \in \mathbb{R}$.

Show that $A^T B - I = C$; where I is the identity matrix of order 2.

Show also that C^{-1} exists **if and only if** $a \neq 0$.

Now, let $a = 1$. Write down C^{-1} .

Find the matrix P such that $CPC = 2I + C$.

(b) Let $z, w \in \mathbb{C}$. Show that $|z|^2 = z\bar{z}$ and applying it to $z - w$,

show that $|z - w|^2 = |z|^2 - 2\operatorname{Re} z\bar{w} + |w|^2$.

Write a similar expression for $|1 - z\bar{w}|^2$ and show that $|z - w|^2 - |1 - z\bar{w}|^2 = -(1 - |z|^2)(1 - |w|^2)$.

Deduce that if $|w| = 1$ and $z \neq w$, then $\left| \frac{z - w}{1 - z\bar{w}} \right| = 1$.

(c) Express $1 + \sqrt{3}i$ in the form $r(\cos \theta + i \sin \theta)$, where $r > 0$ and $0 < \theta < \frac{\pi}{2}$.

It is given that $(1 + \sqrt{3}i)^m (1 - \sqrt{3}i)^n = 2^8$, where m and n are positive integers.

Applying De Moivre's theorem, obtain equations sufficient to determine the values of m and n .

14.(a) Let $f(x) = \frac{x(2x-3)}{(x-3)^2}$ for $x \neq 3$.

Show that $f'(x)$, the derivative of $f(x)$, is given by $f'(x) = \frac{9(1-x)}{(x-3)^3}$ for $x \neq 3$.

Hence, find the interval on which $f(x)$ is increasing and the intervals on which $f(x)$ is decreasing.

Also, find the coordinates of the turning point of $f(x)$.

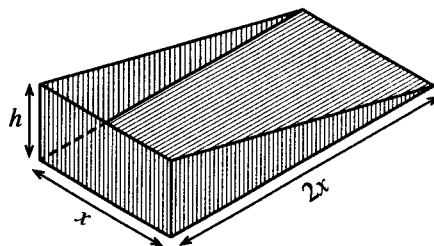
It is **given that** $f''(x) = \frac{18x}{(x-3)^4}$ for $x \neq 3$.

Find the coordinates of the point of inflection of the graph of $y = f(x)$.

Sketch the graph of $y = f(x)$ indicating the asymptotes, the turning point and the point of inflection.

(b) The adjoining figure shows the portion of a dust pan without its handle. Its dimensions in centimetres, are shown in the figure. It is given that its volume $x^2 h \text{ cm}^3$ is 4500 cm^3 .

Its surface area $S \text{ cm}^2$ is given by $S = 2x^2 + 3xh$. Show that S is minimum when $x = 15$.



15.(a) It is given that there exist constants A and B such that

$$x^3 + 13x - 16 = A(x^2 + 9)(x + 1) + B(x^2 + 9) + 2(x + 1)^2 \text{ for all } x \in \mathbb{R}.$$

Find the values of A and B .

Hence, write down $\frac{x^3 + 13x - 16}{(x + 1)^2 (x^2 + 9)}$ in partial fractions and

find $\int \frac{x^3 + 13x - 16}{(x + 1)^2 (x^2 + 9)} dx$.

(b) Using integration by parts, evaluate $\int_0^1 e^x \sin^2 \pi x dx$.

(c) Using the formula $\int_0^a f(x) dx = \int_0^a f(a - x) dx$, where a is a constant,

show that $\int_0^\pi x \cos^6 x \sin^3 x dx = \frac{\pi}{2} \int_0^\pi \cos^6 x \sin^3 x dx$.

Hence, show that $\int_0^\pi x \cos^6 x \sin^3 x dx = \frac{2\pi}{63}$.

16. Let $A \equiv (1, 2)$ and $B \equiv (3, 3)$.

Find the equation of the straight line l passing through the points A and B .

Find the equations of the straight lines l_1 and l_2 passing through A , each making an acute angle $\frac{\pi}{4}$ with l .

Show that the coordinates of any point on l can be written in the form $(1 + 2t, 2 + t)$, where $t \in \mathbb{R}$.

Show also that the equation of the circle C_1 lying entirely in the first quadrant with radius $\frac{\sqrt{10}}{2}$, touching both l_1 and l_2 , and its centre on l is $x^2 + y^2 - 6x - 6y + \frac{31}{2} = 0$.

Write down the equation of the circle C_2 whose ends of a diameter are A and B .

Determine whether the circles C_1 and C_2 intersect orthogonally.

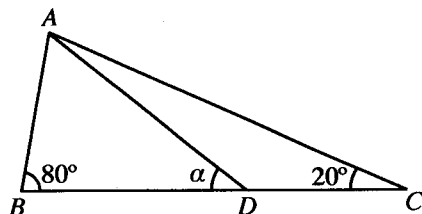
17.(a) Write down $\sin(A-B)$ in terms of $\sin A$, $\cos A$, $\sin B$ and $\cos B$.

Deduce that

(i) $\sin(90^\circ - \theta) = \cos \theta$, and

(ii) $2 \sin 10^\circ = \cos 20^\circ - \sqrt{3} \sin 20^\circ$.

(b) In the usual notation, state the **Sine Rule** for a triangle ABC .



In the triangle ABC shown in the figure, $\hat{A}BC = 80^\circ$ and $\hat{A}CB = 20^\circ$. The point D lies on BC such that $AB = DC$. Let $\hat{A}DB = \alpha$.

Using the **Sine Rule** for suitable triangles, show that $\sin 80^\circ \sin(\alpha - 20^\circ) = \sin 20^\circ \sin \alpha$.

Explain why $\sin 80^\circ = \cos 10^\circ$ and **hence**, show that $\tan \alpha = \frac{\sin 20^\circ}{\cos 20^\circ - 2 \sin 10^\circ}$.

Using the result in (a)(ii) above, **deduce** that $\alpha = 30^\circ$.

(c) Solve the equation $\tan^{-1}(\cos^2 x) + \tan^{-1}(\sin x) = \frac{\pi}{4}$.

නව නිර්දේශය / புதிய பாடத்திட்டம் / New Syllabus

ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව
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 Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka
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 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020
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සංයුක්ත ගණිතය II
 இணைந்த கணிதம் II
 Combined Mathematics II

10 E II

පැය තුනයි
 மூன்று மணித்தியாலம்
 Three hours

අමතර කියවීමේ කාලය - මිනිත්තු 10 යි
 மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள்
 Additional Reading Time - 10 minutes

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- * In this question paper, g denotes the acceleration due to gravity.

For Examiners' Use only

(10) Combined Mathematics II		
Part	Question No.	Marks
A	1	
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	Total	

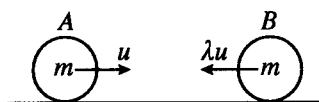
Total

In Numbers	
In Words	

Code Numbers

Marking Examiner	
Checked by:	1
	2
Supervised by:	

1. Two particles A and B each of mass m , moving in the same straight line on a smooth horizontal floor, but in opposite directions collide directly. The velocities of A and B just before collision are u and λu , respectively. The coefficient of restitution between A and B is $\frac{1}{2}$.

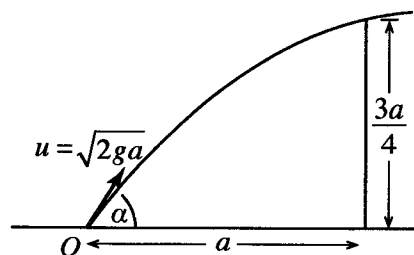


Find the velocity of A just after collision and show that if $\lambda > \frac{1}{3}$, then the direction of motion of A is reversed.

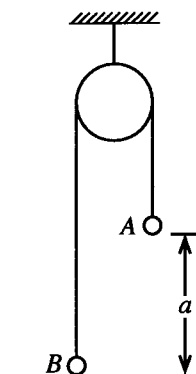
2. A particle is projected from a point O on a horizontal floor with initial velocity $u = \sqrt{2ga}$ and at an angle α ($0 < \alpha < \frac{\pi}{2}$) to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance a from O .

Show that $\sec^2 \alpha - 4 \tan \alpha + 3 = 0$.

Hence, show that $\alpha = \tan^{-1}(2)$.

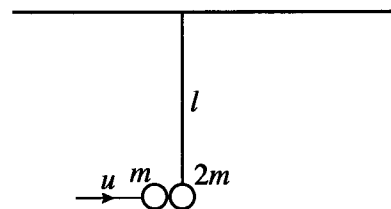


3. Two particles A and B , each of mass m , attached to the two ends of a light inextensible string which passes over a fixed smooth pulley are in equilibrium with the particle A at a height a from a horizontal floor and the particle B touching the floor, as shown in the figure. Now, the particle A is given an impulse mu vertically downwards. Find the velocity of the particle A just after the impulse. Write down the time taken by A to reach the floor.



4. A car of mass 1500 kg travels on a straight horizontal road against a constant resistance of magnitude 500 N . Find the acceleration of the car when the engine of the car is working at power 50 kW and the car is travelling with speed 25 m s^{-1} .
At this instant, the engine of the car is turned off. Find the speed of the car after 50 seconds from the instant the engine was turned off.

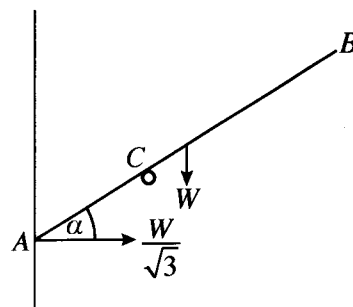
5. A particle P of mass $2m$, hanging freely from a horizontal ceiling by a light inextensible string of length l , is in equilibrium. Another particle of mass m moving in a horizontal direction with velocity u collides with the particle P and coalesces to it. The string remains taut after the collision and the composite particle just reaches the ceiling. Show that $u = \sqrt{18gl}$.



6. Let $\alpha > 0$ and in the usual notation, let $\mathbf{i} + \alpha\mathbf{j}$ and $\alpha\mathbf{i} - 2\mathbf{j}$ be the position vectors of two points A and B , respectively, with respect to a fixed origin O . Also, let C be the point on AB such that $AC : CB = 1 : 2$. It is given that OC is perpendicular to AB . Find the value of α .

7. A uniform rod ACB of length $2a$ and weight W is kept in equilibrium with the end A against a smooth vertical wall by a smooth peg placed at C , as shown in the figure. It is given that the reaction at A from the wall is $\frac{W}{\sqrt{3}}$. Show that the angle α that the rod makes with the horizontal is $\frac{\pi}{6}$.

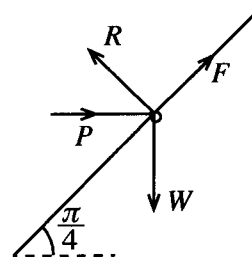
Show also that $AC = \frac{3}{4}a$.



8. A small bead of weight W is threaded to a fixed rough straight wire inclined at an angle $\frac{\pi}{4}$ to the horizontal. The bead is kept in equilibrium by a horizontal force of magnitude P as shown in the figure. The coefficient of friction between the bead and the wire is $\frac{1}{2}$.

Obtain equations sufficient to determine the frictional force F and the normal reaction R on the bead, in terms of P and W .

It is **given** that $\frac{F}{R} = \frac{W-P}{W+P}$. Show that $\frac{W}{3} \leq P \leq 3W$.



9. Let A and B be two events of a sample space Ω . In the usual notation, it is given that $P(A) = \frac{3}{5}$, $P(B|A) = \frac{1}{4}$ and $P(A \cup B) = \frac{4}{5}$. Find $P(B)$.

Show that the events A and B are **not** independent.

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10. A set of 5 observations of positive integers, each less than or equal to 10, has mean, median and mode each equals to 6. The range of the observations is 9. Find these five observations.

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නව නිර්දේශය/புதிய பாடத்திட்டம்/New Syllabus

NEW இலங்கைப் பரீட்சைத் திணைக்களம், Sri Lanka Department of Examinations, Sri Lanka
இலங்கைப் பரீட்சைத் திணைக்களம், Sri Lanka Department of Examinations, Sri Lanka
இலங்கைப் பரීட்சைத் திணைக்களம், Sri Lanka Department of Examinations, Sri Lanka
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අධ්‍යයන පොදු සහතික පත්‍ර (උසස් පෙළ) විභාගය, 2020
கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020
General Certificate of Education (Adv. Level) Examination, 2020

සංයුක්ත ගණිතය **II**
இணைந்த கணிதம் **II**
Combined Mathematics II

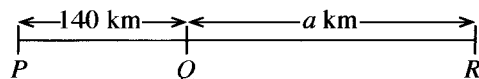
10 E II

Part B

* Answer five questions only.

(In this question paper, g denotes the acceleration due to gravity.)

11. (a) Three railway stations P , Q and R located in a straight line such that $PQ = 140$ km and $QR = a$ km, as shown in the figure. At time $t = 0$, a train A starts from rest



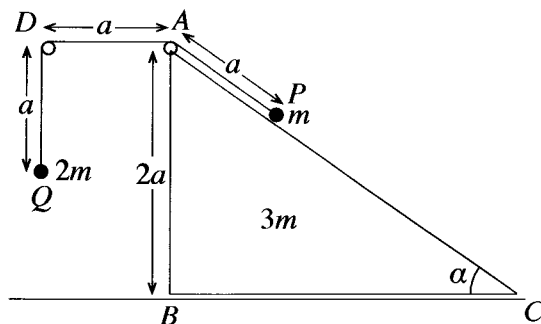
at P and moves towards Q with constant acceleration f km h⁻² for half an hour and maintains the velocity it had at time $t = \frac{1}{2}$ h for three hours. Then it moves with constant retardation f km h⁻² and comes to rest at Q . At time $t = 1$ h, another train B starts from rest at R and moves towards Q with constant acceleration $2f$ km h⁻² for T hours and then with a constant retardation f km h⁻² and comes to rest at Q . Both trains come to rest at the same instant. Sketch velocity-time graphs for the motions of A and B in the same diagram.

Hence or otherwise, show that $f = 80$ and find the values of T and a .

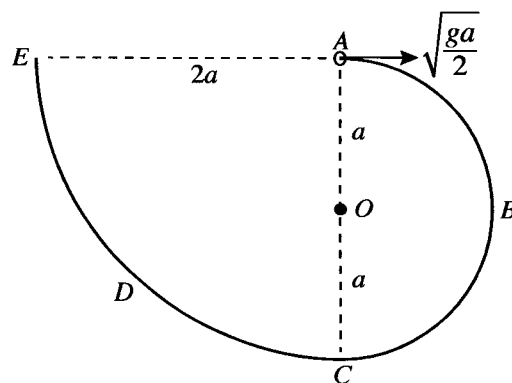
- (b) A ship is sailing due west with uniform speed u relative to earth and a boat is sailing in a straight line path with uniform speed $\frac{u}{2}$ relative to earth. At a certain instant, the ship is at a distance d at an angle $\frac{\pi}{3}$ east of north from the boat.

- (i) If the boat is sailing relative to earth in the direction making an angle $\frac{\pi}{6}$ west of north, show that the boat can intercept the ship and that the time taken by the boat to intercept the ship is $\frac{2d}{\sqrt{3}u}$.
- (ii) If the boat is sailing relative to earth in the direction making an angle $\frac{\pi}{6}$ east of north, show that the speed of the boat relative to the ship is $\frac{\sqrt{7}u}{2}$ and that the shortest distance between the ship and the boat is $\frac{d}{2\sqrt{7}}$.

12. (a) The triangle ABC in the figure is the vertical cross-section through the centre of gravity of a smooth uniform wedge of mass $3m$ with $\hat{ACB} = \alpha$, $\hat{ABC} = \frac{\pi}{2}$ and $AB = 2a$ such that the face containing BC is placed on a smooth horizontal floor. The line AC is a line of greatest slope of the face containing it. The point D is a fixed point in the plane of ABC such that AD is horizontal. Two particles P and Q of masses m and $2m$, respectively are attached to the two ends of a light inextensible string of length $3a$ passing over smooth small pulleys fixed at A and D . The system is released from rest with the particle P held on AC and the particle Q hanging freely such that $AP = AD = DQ = a$, as shown in the figure. Obtain equations sufficient to determine the time taken by the particle Q to reach the floor.



- (b) A smooth thin wire $ABCDE$ is fixed in a vertical plane, as shown in the figure. The portion ABC is a semicircle with centre O and radius a , and the portion CDE is a quarter of a circle with centre A and radius $2a$. The points A and C lie on the vertical line through O and the line AE is horizontal. A small smooth bead P of mass m is placed at A and is given a velocity $\sqrt{\frac{ga}{2}}$ horizontally, and begins to move along the wire.

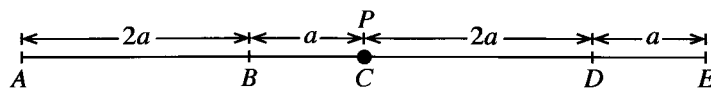


Show that the speed v of the bead P when \overrightarrow{OP} makes an angle θ ($0 \leq \theta \leq \pi$) with \overrightarrow{OA} is given by $v^2 = \frac{ga}{2}(5 - 4\cos\theta)$.

Find the reaction on the bead P from the wire at the above position and show that it changes its direction when the bead P passes the point $\theta = \cos^{-1}\left(\frac{5}{6}\right)$.

Write down the velocity of the bead P just before it leaves the wire at E and find the reaction on the bead P from the wire at that instant.

13. The points A, B, C, D and E lie on a straight line in that order, on a smooth horizontal table such that $AB = 2a$, $BC = a$, $CD = 2a$ and $DE = a$, as shown in the figure. One end of a light elastic string of natural length $2a$ and modulus of elasticity kmg is attached to the point A and the other end to a particle P of mass m . One end of another light elastic string of natural length a and modulus of elasticity mg is attached to the point E and the other end to the particle P . When the particle P is held at C and released, it stays in equilibrium. Find the value of k .



Now, the string AP is pulled until the particle P reaches the point D and released from rest. Show that the equation of motion of P from D to B is given by $\ddot{x} + \frac{3g}{a}x = 0$, where $CP = x$.

Using the formula $\dot{x}^2 = \frac{3g}{a}(c^2 - x^2)$, where c is the amplitude, show that the velocity of particle P when it reaches B is $3\sqrt{ga}$.

An impulse is given to the particle P when it reaches B so that the velocity of P just after the impulse is \sqrt{ag} in the direction of \overrightarrow{BA} .

Show that the equation of motion of P after passing B until it comes to instantaneous rest is given by $\ddot{y} + \frac{g}{a}y = 0$, where $DP = y$.

Show that the total time taken by the particle P , started at D , to reach B for the second time is

$$2\sqrt{\frac{a}{g}}\left(\frac{\pi}{3\sqrt{3}} + \cos^{-1}\left(\frac{3}{\sqrt{10}}\right)\right).$$

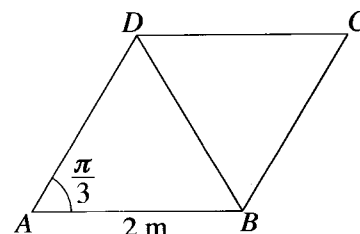
14. (a) Let \mathbf{a} and \mathbf{b} be two **unit vectors**.

The position vectors of three points A , B and C with respect to an origin O , are $12\mathbf{a}$, $18\mathbf{b}$ and $10\mathbf{a} + 3\mathbf{b}$ respectively. Express \overrightarrow{AC} and \overrightarrow{CB} in terms of \mathbf{a} and \mathbf{b} .

Deduce that A , B and C are collinear and find $AC:CB$.

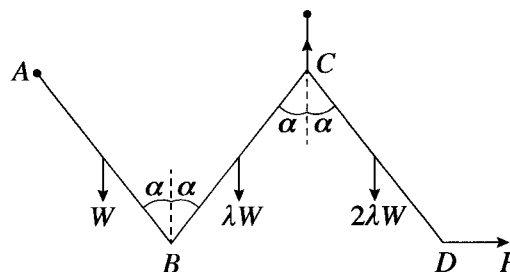
It is given that $OC = \sqrt{139}$. Show that $\angle AOB = \frac{\pi}{3}$.

- (b) Let $ABCD$ be a rhombus with $AB = 2$ m and $\angle BAD = \frac{\pi}{3}$. Forces of magnitude 10 N, 2 N, 6 N, P N and Q N act along AD , BA , BD , DC and CB respectively, in the directions indicated by the order of the letters. It is given that the resultant force is of magnitude 10 N and its direction is in the direction parallel to BC in the sense from B to C . Find the values of P and Q . Also, find the distance from A to the point where the line of action of the resultant force meets BA produced.



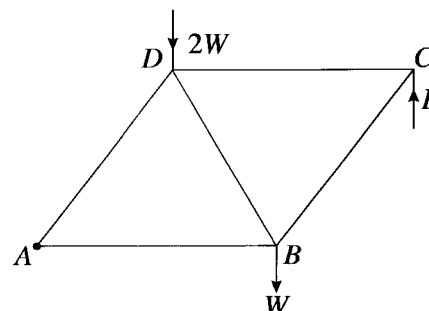
Now, a couple of moment M Nm acting in the counterclockwise sense and two forces, each of magnitude F N acting along CB and DC in the directions indicated by the order of the letters, are added to the system so that the resultant force passes through the points A and C . Find the values of F and M .

15. (a) Three uniform rods AB , BC and CD , each of length $2a$ are smoothly joined at the ends B and C . The weights of the rods AB , BC and CD are W , λW and $2\lambda W$, respectively. The end A is smoothly hinged to a fixed point. The rods are kept in equilibrium in a vertical plane by a light inextensible string attached to the joint C and to a fixed point vertically above C and by a horizontal force P applied to the end D such that A and C are at the same horizontal level and each of the rods making an angle α with the vertical, as shown in the figure. Show that $\lambda = \frac{1}{3}$.



Show also that the horizontal and vertical components of the force exerted on AB by CB at B are $\frac{W}{3}\tan\alpha$ and $\frac{W}{6}$, respectively.

- (b) The framework shown in the adjoining figure is made from light rods AB , BC , CD , DA and BD , each of length $2a$, freely jointed at A , B , C and D . There are loads of W and $2W$ at B and D , respectively. The framework is smoothly hinged at A to a fixed point and kept in equilibrium with AB horizontal by a vertical force P applied to it at C , as shown in the figure. Find the value of P in terms of W .

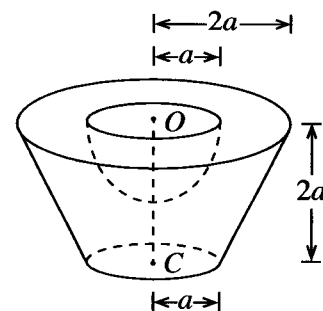


Draw a stress diagram using Bow's notation and **hence**, find the stresses in the rods stating whether they are tensions or thrusts.

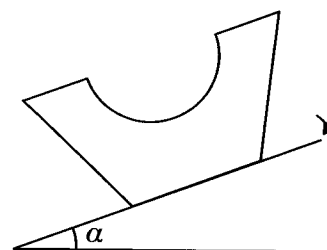
16. Show that the centre of mass of

- (i) a uniform solid right circular cone of base radius r and height h is at a distance $\frac{h}{4}$ from the centre of the base,
- (ii) a uniform solid hemisphere of radius r is at a distance $\frac{3r}{8}$ from its centre.

The adjoining figure shows a mortar S made by removing a solid hemisphere from a frustum of a solid uniform right circular cone having base radius $2a$ and height $4a$. The radius and the centre of the upper circular face of the frustum are $2a$ and O , respectively, and those for the lower circular face are a and C , respectively. The height of the frustum is $2a$. The radius and the centre of the removed solid hemisphere are a and O , respectively. Show that the centre of mass of mortar S lies at a distance $\frac{41}{48}a$ from O .



Mortar S is placed on a rough horizontal plane with its lower circular face touching the plane. Now, the plane is tilted upwards slowly. The coefficient of friction between the mortar and the plane is 0.9. Show that if $\alpha < \tan^{-1}(0.9)$, then the mortar stays in equilibrium, where α is the inclination of the plane to the horizontal.



- 17.(a) In a certain factory, machine A makes 50% of the items and the rest are made by machines B and C. It is known that 1%, 3% and 2% of the items made by A, B and C respectively are defective. The probability that a randomly selected item is defective is given to be 0.018. Find the percentages of items made by the machines B and C.

Given that a randomly selected item is defective, find the probability that it was made by the machine A.

- (b) The time taken (in minutes) to travel to work from their homes of 100 employees of a certain factory are given in the following table:

Time taken	Number of employees
0 – 20	10
20 – 40	30
40 – 60	40
60 – 80	10
80 – 100	10

Estimate the mean, standard deviation and the mode of the distribution given above.

Later, all of the employees in the class interval 80 – 100 moved closer to the factory. It has changed the frequency of the class interval 80 – 100 from 10 to 0 and the frequency of the class interval 0 – 20 from 10 to 20.

Estimate the mean, standard deviation and the mode of the new distribution.

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